Partial Sampling Operator and Structural Distance Ranking for Multi-Objective GP

> Makoto OHKI Tottori University, Japan

#### Applications of Genetic Programming (GP)

- Program Synthesis
- Function Generation
- Rule Set Discovery



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#### Program Synthesis [David2017]

```
type list = Nil | Cons of int * list
let rec even x =
  match x with
  | Nil -> Nil
  | Cons(u, Nil) -> Cons(u, Nil)
  | Cons(u, Cons(_, us))
     -> Cons(u, even us)
let rec sum x =
  match x with
  | Nil -> 0
  | Cons(u, us) -> u + sum us
let rec sum_even = ??
let main x = assert (sum (even x) = sum_even x)
```



#### 1.Introduction

2.MOGP with SD

3. Partial Sampling

4.Verification

5.Conclusion

let rec sum\_even x = match x with | Nil -> o | Cons (u, Nil) -> u | Cons (u, Cons(\_, us)) -> u + sum\_even us

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#### • Function Generation [Jamali2017]











They can be expressed by a tree structure data.





2.MOGP with SD

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Genetic Programming: GP

In this paper,



- index of goodness of the tree
- the Size of the tree
- tree position in the population by Structural Distance (SD)

Apply SD instead of Crowding Distance (CD) of NSGA-II

Partial Sampling (PS) operator instead of Crossover and Mutation

Double Spiral Problem for verification



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### Objective Functions

1 objective function according to Goodness of the tree structure

 $h_1(\text{indiv}_i) = \text{performance}(\text{root}_i)$ 

2 objective function according to the size of the tree structure

 $h_2(\text{indiv}_i) = \frac{1}{\text{size}(\text{root}_i)}$ 

③ objective function according to average of SD in the population

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$$h_3(\text{indiv}_i) = \frac{1}{N_{\text{pop}}} \sum_{k=1}^{N_{\text{pop}}} \text{SD indiv}_i, \text{indiv}_k$$

#### Structural Distance (SD)





#### Structural Distance (SD)



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NSGA-II



NSGA-II with SD instead of CD



Proliferation in Partial Sampling (PS) Operator



• Proliferation Terminate Probability  $p_t$ 

$$p_t^0 = \frac{1}{\text{AverageSize } \mathbf{R}^g}$$

$$p_t^{g+1} = \frac{\operatorname{Succ} \mathbf{R}^g - p_t^0 \cdot \operatorname{Succ} \mathbf{P}^g}{\operatorname{Succ} \mathbf{P}^g - p_t^0 \cdot \operatorname{Succ} \mathbf{R}^g} p_t^g - p_t^0 + p_t^0$$

<b>R</b> <sup>g</sup>	: population
$\mathbf{P}^{g}$	: parents



#### 2 kinds of metastasis





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 $\begin{cases} f(x, y) > 0 \Leftrightarrow (x, y) \in \mathbf{D}_1 \\ f(x, y) < 0 \Leftrightarrow (x, y) \in \mathbf{D}_2 \\ f(x, y) = 0 \Leftrightarrow \text{FALSE} \end{cases}$ 

#### difficult even by the neural network.



 $\circ$  non-terminal node  $\in$  +, -, \*,  $\div$ , sin, cos, tan, ifltz

 $\circ$  terminal node  $\in x, y$ , constant

if 
$$\operatorname{ifltz}(a,b,c) \triangleq \operatorname{if} a < 0$$
 then b else c  
=  $\begin{cases} b & (a < 0) \\ c & (\text{otherwise}) \end{cases}$ 

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igodow Objective function  $h_1$  according to the goodness of tree

$$h_{1}(\operatorname{indiv}_{i}) = \operatorname{performance}(\operatorname{root}_{i}) = \frac{1}{|\mathbf{D}_{1} \cup \mathbf{D}_{2}|} \sum_{k=1}^{|\mathbf{D}_{1} \cup \mathbf{D}_{2}|} \frac{g(x_{k}, y_{k})}{|\mathbf{D}_{1}|}$$

$$g(x, y) = \begin{cases} 1 & f(x, y) > 0 \land (x, y) \in \mathbf{D}_{1} \\ 0 & f(x, y) > 0 \land (x, y) \in \mathbf{D}_{2} \\ 1 & f(x, y) < 0 \land (x, y) \in \mathbf{D}_{2} \\ 0 & f(x, y) < 0 \land (x, y) \in \mathbf{D}_{1} \\ 0 & f(x, y) = 0 \end{cases}$$

1.Introduction2.MOGP with SD3.Partial Sampling4.Verification5.Conclusion

#### Final Solution Distribution





1.Introduction

2.MOGP with SD

5.Conclusion

Comparison among 3-Objective, 2-Objective, 1-Objective GPs



Comparison of results on MS-Norm plane



# 5. Conclusion

In this paper,

Multi-Objective GP
 In addition to goodness of the tree, 2 objective functions

 tree size
 Structural Distance (SD)

 Partial Sampling (PS) for mating

Double Spiral Problem for verification.

• The proposed technique (PS + SD  $\rightarrow$  NSGA-II) is effective.

1.Introduction	
2.MOGP with SD	
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# 5. Conclusion

In the future,

Enhance the capability of numerical optimization

Ranking Selection technique harmonizing CD and SD

Mechanism to forcibly exit from PS



Thank you very much!

Ask me simply, if you have.



degree of spread of  $\mathcal{FFS}$ 

$$MS = \sqrt{\sum_{i=1}^{\mathcal{M}} \begin{pmatrix} |\mathcal{FFS}| & |\mathcal{FFS}| \\ \max_{j=1} f_i(\mathbf{x}_j) - \min_{j=1} f_i(\mathbf{x}_j) \end{pmatrix}^2}$$

#### degree of convergence to $\mathcal{POS}$

Norm = 
$$\frac{1}{|\mathcal{FFS}|} \sum_{j=1}^{|\mathcal{FFS}|} \sqrt{\sum_{i=1}^{m} f_i(\mathbf{x}_j)^2}$$

#### 2 kinds of metastasis

